

Logic Circuits

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Chapter_ 1

Digital Concepts

Lecture _01

Digital Basics

Syllabus Outline

| No_Ch | Title | Contents |
|-------|---|--|
| Ch_1 | Introductory Concepts | Digital and Analog Quantities, Binary Digits, Logic Levels, Digital Waveforms, Basic Logic Functions |
| Ch_2 | Number Systems, Operations, and Codes | Decimal, Binary, Complements, Hexadecimal, Octal, Binary Coded Decimal (BCD) and Digital Codes |
| Ch_3 | Logic Gates | AND, OR, NAND, NOR, Exclusive-OR and Exclusive-NOR |
| Ch_4 | Boolean Algebra and Logic Simplification | Operations and Expressions, Laws and Rules, DeMorgan's Theorems, Truth Tables and Karnaugh Map |
| Ch_5 | Combinational Circuit Analysis | Basic Combinational Logic Circuits, Implementing Combinational Logic, Combinational Logic Using NAND and NOR Gates, Pulse Waveform Operation |
| Ch_6 | Functions of Combinational Logic | Adders, Comparators, Decoders, Encoders, Multiplexers and Demultiplexers. |
| Ch_7 | Sequential circuit analysis | Latches, Flip-Flops, and Timers. Shift Registers. Counters |

Intended Learning Outcomes

After completing the course, the student will be able to:

- Understand number systems, codes, and binary arithmetic.
- Produce the truth table, timing diagram.
- Use Boolean Algebra, recognize Operator precedence.
- Use standard forms and simplify of Boolean functions.
- Construct Karnaugh Maps.
- Design combinational circuits.
- Build and trace the logic of circuits composed of simple gates.
- Describe the behavior of the following circuits: Adders, comparators, Decoder, Encoder, Multiplexer, Flip-Flops, registers, and Counters.
- Analyze synchronous sequential circuits.

Assessment

| | |
|--|----------------|
| Coursework: | 50% |
| Activity | 10% |
| 2 Tests | 20% (10% each) |
| Practice | 20% |
| Examination: | 50% |
| To pass the course, at least 25% of coursework AND examination marks are required. | |

Text book

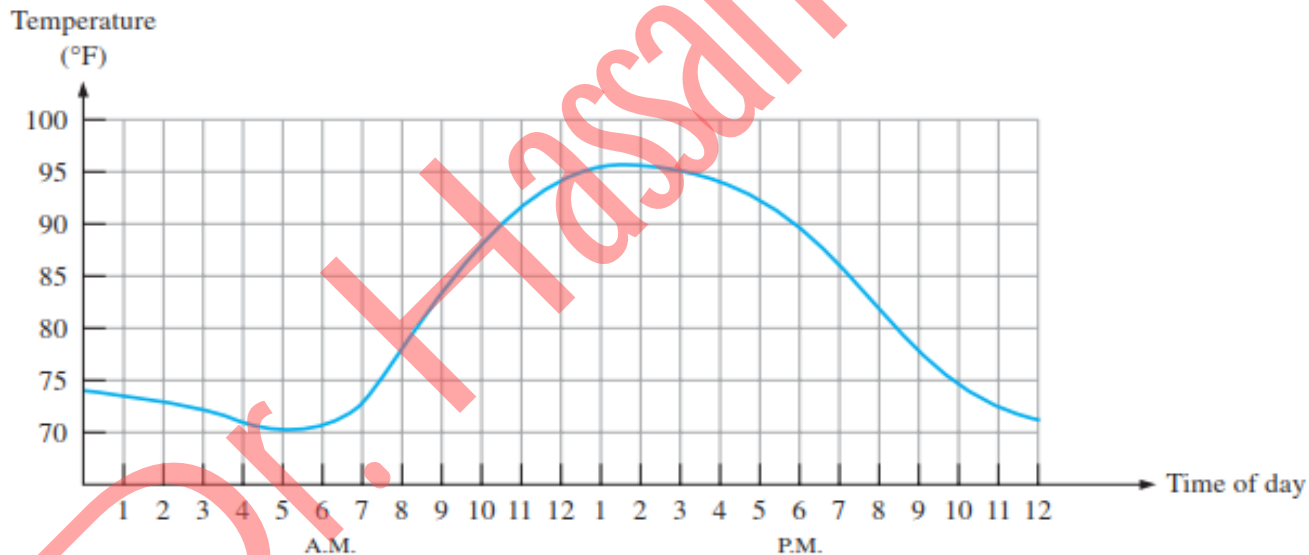
1. Thomas L. Floyd. Digital Fundamentals, (9,10) 11-th Edition, Pearson Education Limited 2015.

References

1. Morris Mano. Digital design, 4-th edition, Pearson Education, 2007.
2. Fundamentals of Digital Logic Design with Verilog Design, S. Brown and Z. Vranesic, McGraw Hill Ed., 2003.
3. أ. د. محمد ابراهيم العدوي. الدوائر المنطقية. قسم الإلكترونيات والاتصالات والحاسبات، كلية الهندسة – جامعة حلوان.

1-1. Digital and Analog Quantities (الكميات الرقمية والتماثلية)

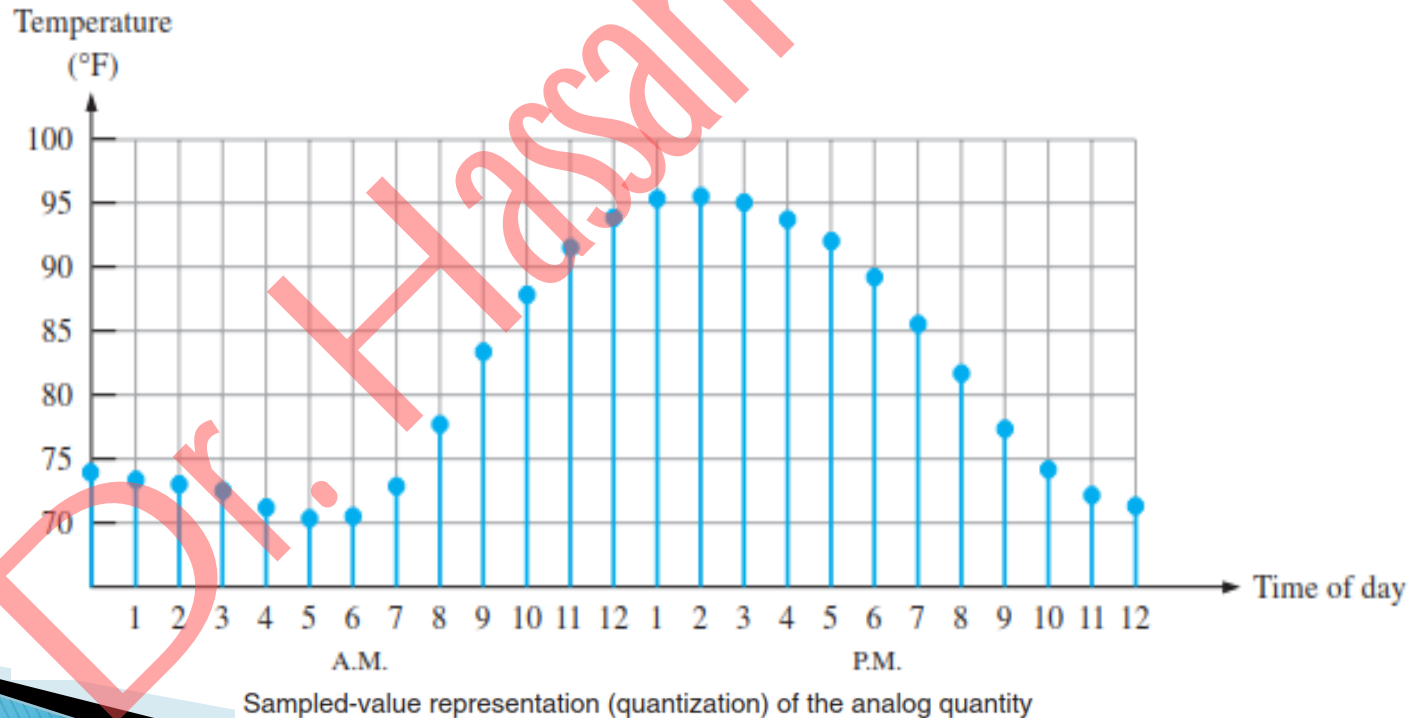
- An **analog** quantity is one having **continuous values**.
- A **digital** quantity is one having a **discrete set** of values.
- Most **natural quantities** that we see are **analog** and vary **continuously**.
- For example, the air **temperature changes** over a **continuous range** of values as shown in Fig.



Graph of an analog quantity (temperature versus time).

Digital and Analog Quantities

- **Analog systems** can generally handle (تتعامل) **higher power** than **digital systems**.
- **Digital systems** can **process, store, and transmit data** more **efficiently** but can only assign (تُخصّص) **discrete values** to each point.
- **For example**, have **sampled values** (قيم متقطعة = عينات) representing the temperature at **discrete points in time** (every hour) over a 24-hour period, as indicated in Fig.

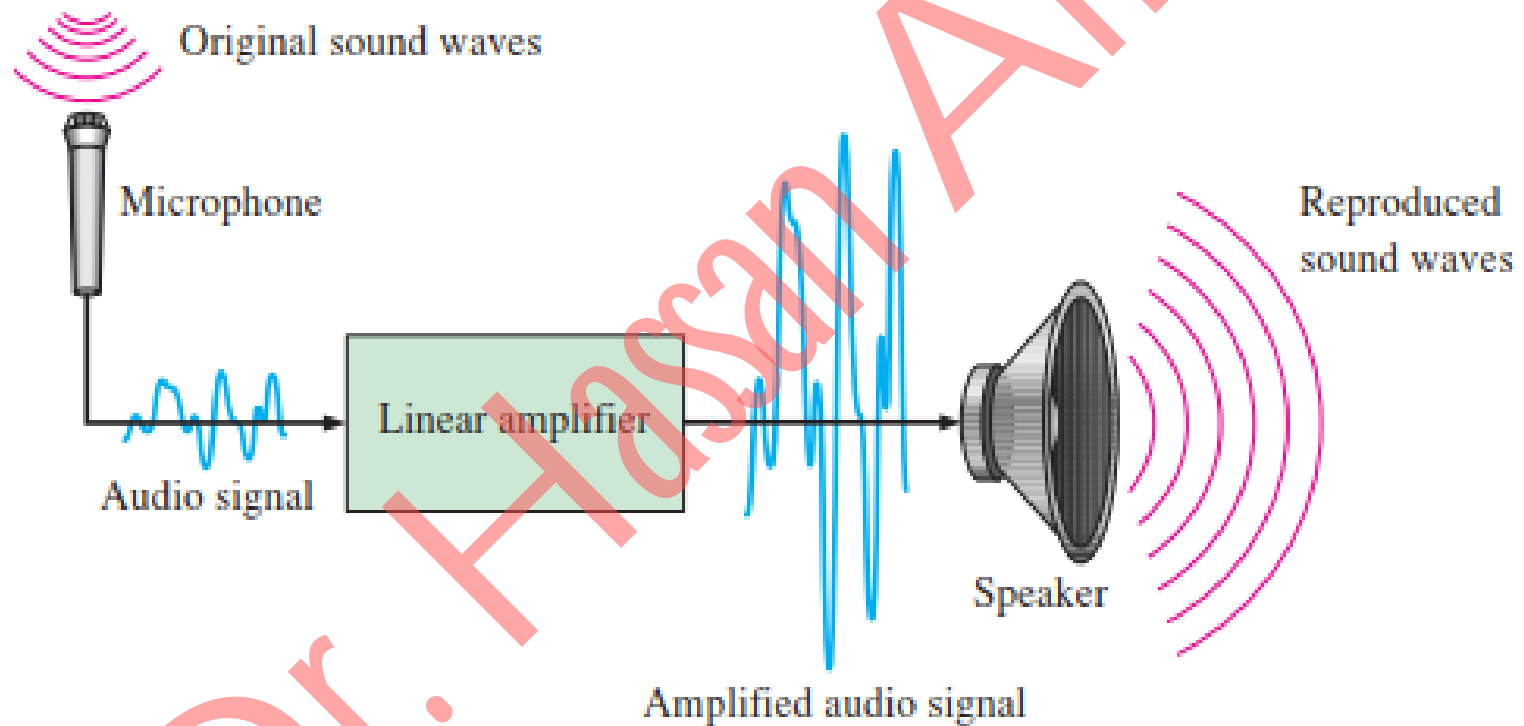


The digital advantage (مميزات التمثيل الرقمي)

- Digital data can be processed and transmitted more efficiently (أكثر كفاءة) and reliable (موثوقة) than analog data.
- Digital data has a great advantage when storage is necessary.
- For example,
 - Music when converted to digital form can be stored more compactly and reproduced with greater accuracy (دقة) and clarity than is possible when it is in analog form.
 - Noise (unwanted voltage fluctuations (تقلبات)) does not affect digital data nearly as much as it does analog signals.

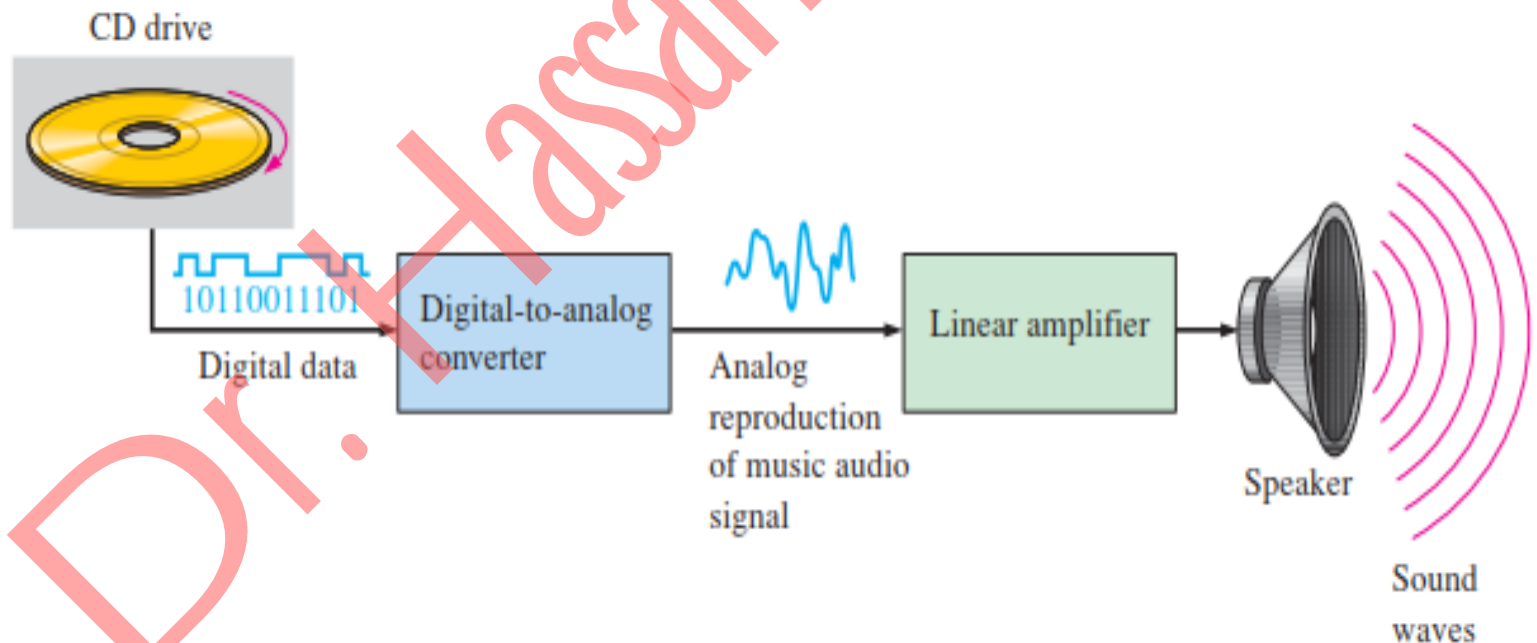
Analog System

- A **public address system**, used to **amplify sound**, is one simple example of an application of analog electronics, shown in Fig.



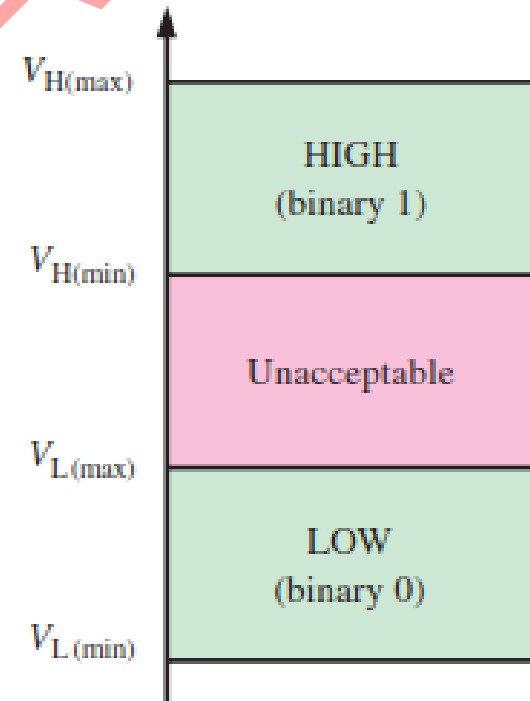
A System Using Digital and Analog Methods

- The **compact disk (CD) player** is an example of a system in which both **digital** and **analog** circuits are used, shown in Fig.
 - A **laser diode optical system** picks up the **digital data** from the rotating disk and **transfers** it to the **digital-to-analog converter (DAC)**.
- When the music was originally **recorded on the CD**, a process, essentially the **reverse** of the one described here, using an **analog-to-digital converter (ADC)** was used.



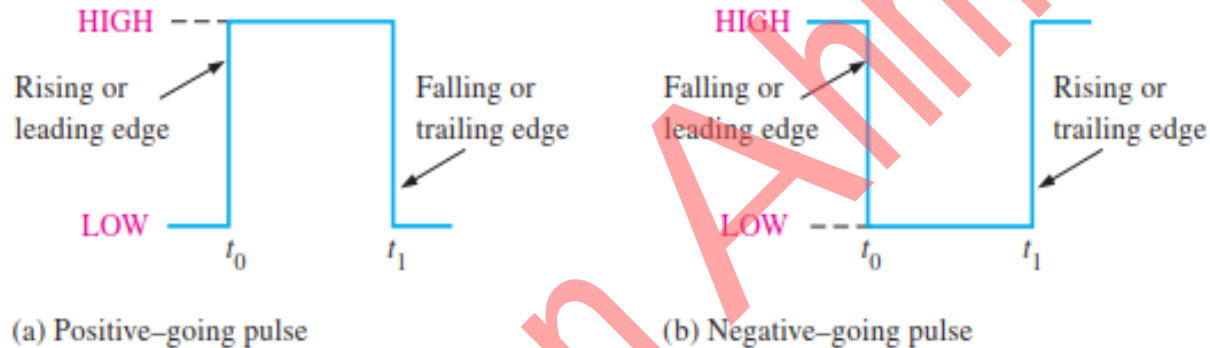
1-2. Binary Digits, Logic Levels and Digital Waveforms

- **Digital electronics** uses circuits that have **two states**, which are represented by two different **voltage levels** called **HIGH** and **LOW**.
- The **voltages** represent **numbers** in the **binary system**.
- In **binary**, a single number is called a **bit** (for **binary digit**).
- A **bit** can have the value of either a **0** or a **1**, depending on if the voltage is **HIGH** or **LOW**.



Digital Waveforms (الموجات الرقمية)

- **Digital waveforms** change between the **LOW** and **HIGH** levels, as shown in Fig.



- 1) A **positive-going pulse** (نبضة موجبة الاتجاه) is one that goes from a normally **LOW logic level** to a **HIGH** level and then back again.
 - 2) A **negative-going pulse** (نبضة سالبة الاتجاه) is one that goes from a normally **HIGH logic level** to a **LOW** level and then back again.
- Digital waveforms are made up of a **series of pulses**.
 - Pulse has **two edges**: a **leading edge** (حافة أمامية) that occurs first at time t_0 and a **trailing edge** (حافة خلفية) that occurs last at time t_1 .
 - The pulses in Fig. are **ideal** because the **rising** (صاعدة) and **falling** (هابطة) edges are assumed to change in **zero time** (instantaneously (لحظي)).

Pulse Definitions (تفاصيل النبضة)

Actual pulses are **not ideal** but are described by:

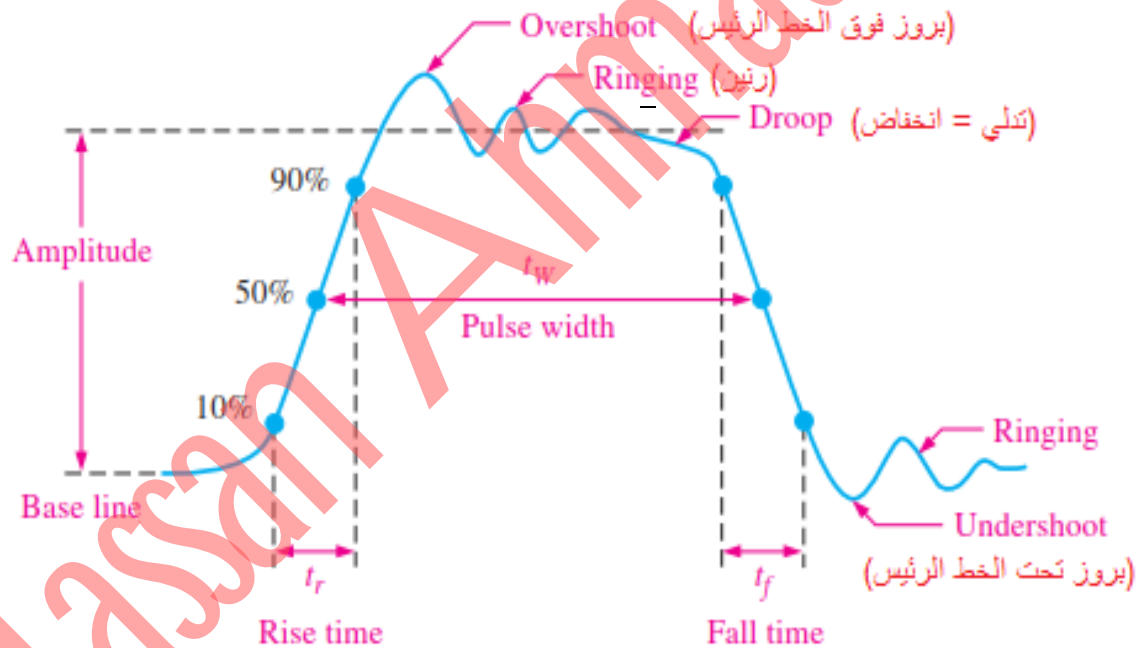
1) **Rise time (t_r)** (زمن الصعود):

the time required for a pulse to go from its **LOW** level to its **HIGH** level. (from 10% of the **pulse amplitude** (مطال = ارتفاع) (height from baseline) to 90%).

2) **Fall time (t_f)** (زمن الهبوط):

the time required for the **transition** from the **HIGH** level to the **LOW** level. (from 90% to 10% of the pulse amplitude).

3) **Pulse width (t_w)** (عرض النبضة) or (*pulse active time*) is a measure of the **duration** of the **pulse** and is often defined as the **time interval** between the **50% points** on the **rising** and **falling** edges.

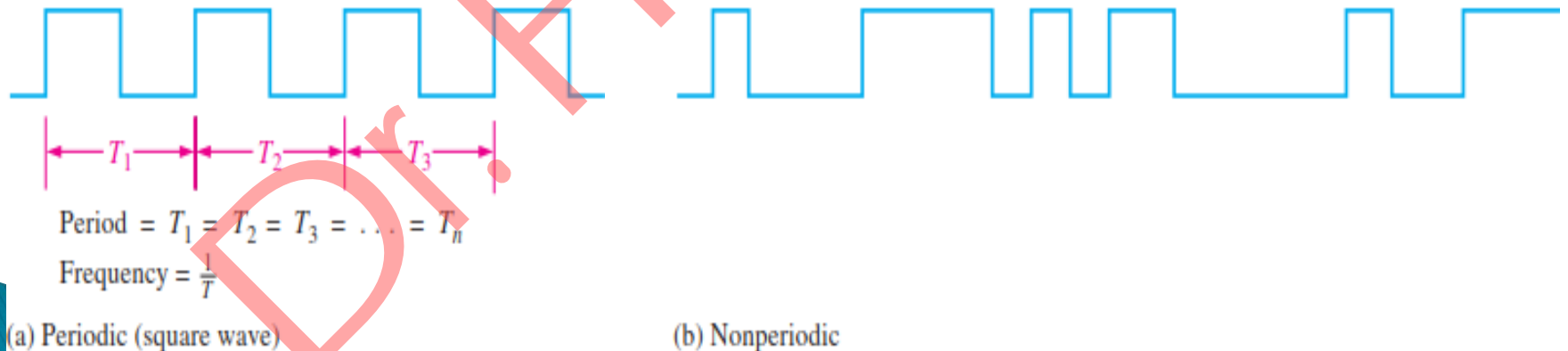


Waveforms characteristics (خصائص الموجات)

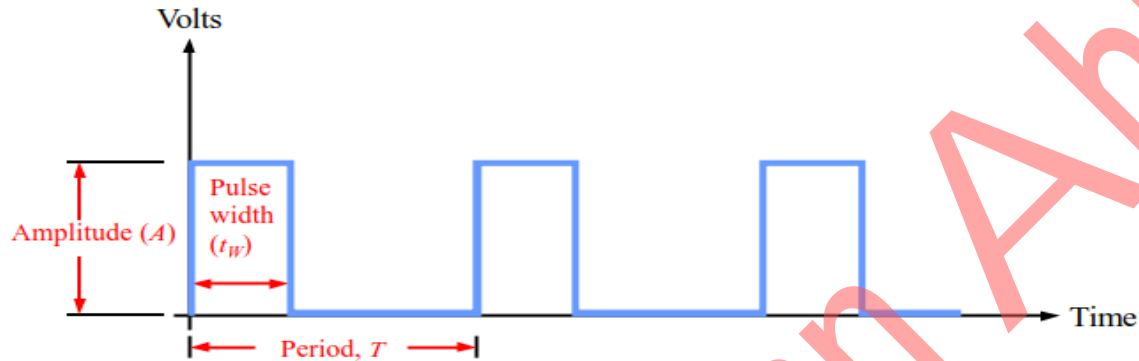
- Most waveforms encountered in digital systems are composed of series of pulses, sometimes called **pulse train** (قطار النبضة), and can be classified as either periodic or nonperiodic.
 - A **periodic pulse** waveform is one that repeat itself at a fixed interval, called a **period** (T). The **frequency** (f) is the **rate** (المعدل/النسبة) at which a pulse repeats itself and measured in **hertz** (**Hz**).

$$f = \frac{1}{T} \quad \text{or} \quad T = \frac{1}{f}$$

- A **nonperiodic pulse** waveform, of course, does not repeat itself at fixed intervals and may be composed of pulses of randomly differing pulse width and/or randomly differing time intervals between the pulses.

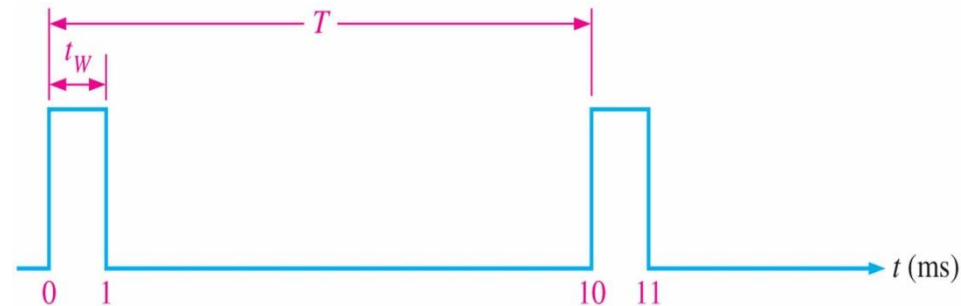


- In addition to **frequency** and **period**, repetitive pulse waveforms are described by the **amplitude** (A), **pulse width** (t_w) and **duty cycle** (دورة العمل).
- **Duty cycle** is the ratio of t_w to T . It can be represents as percentage.



$$\text{Duty cycle} = \left(\frac{t_w}{T} \right) 100\%$$

Example 1-1 A portion of periodic digital waveform is shown in Fig. The measurements are in milliseconds. Determine the following: period, frequency and duty cycle.



$$T = 10\text{ms};$$

$$f = \frac{1}{T} = \frac{1}{10\text{ms}} = 100\text{Hz}$$

$$\text{Duty cycle} = \left(\frac{t_w}{T} \right) 100\% = \left(\frac{1\text{ms}}{10\text{ms}} \right) 100\% = 10\%$$

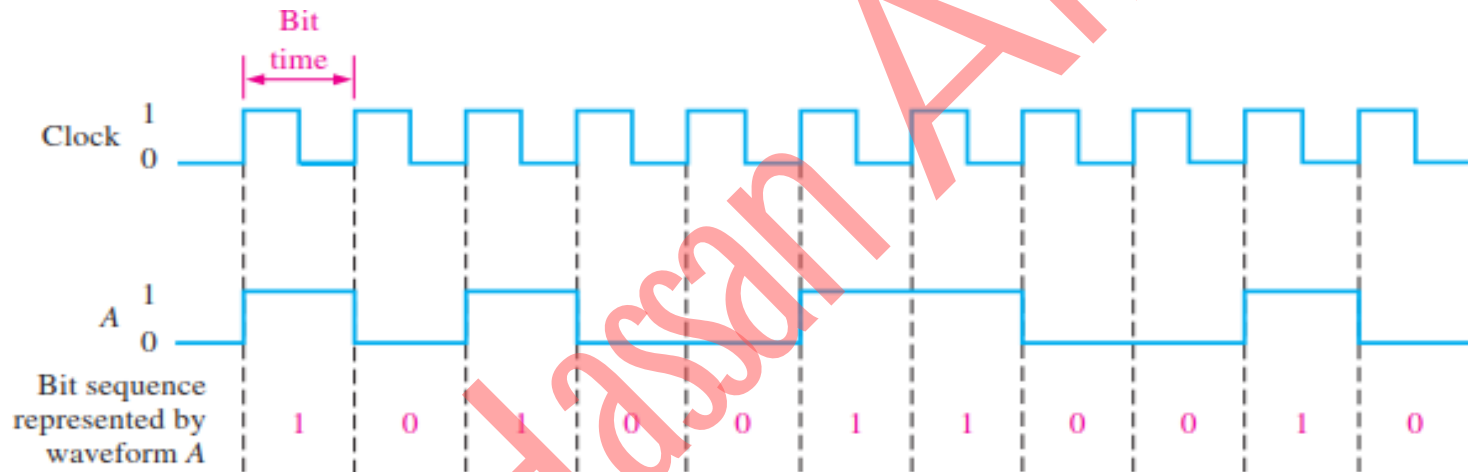
نسبة الدورة الواحدة من الإشارة 10% من إجمالي الإشارة الذي قد يكون ثانية ، أو يوما ، أو حتي أسبوع

A digital waveforms Carries Binary Information

The clock

- In digital systems, all waveforms are synchronized with a basic timing waveform called the **clock**, that is a periodic waveform, and itself **does not carry information**.

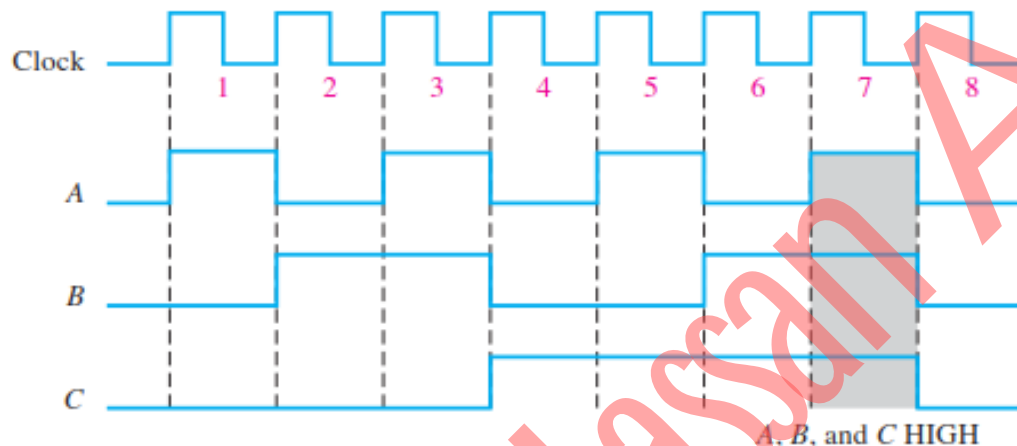
An example of clock is shown in Fig.



- In this case, each **change** in level of **waveform A** occurs at the **leading edge** of the clock waveform.
- In other cases, **level changes** occur at the **trailing edge** of clock.
- During each **bit time** of the clock, **waveform A** is either **HIGH** or **LOW**.
- These **HIGHs** and **LOWs** represent a **sequence of bits**.
- A **group** of **several bits** can be used as **piece of binary information**, such as a **number** or a **letter**.

Timing Diagrams

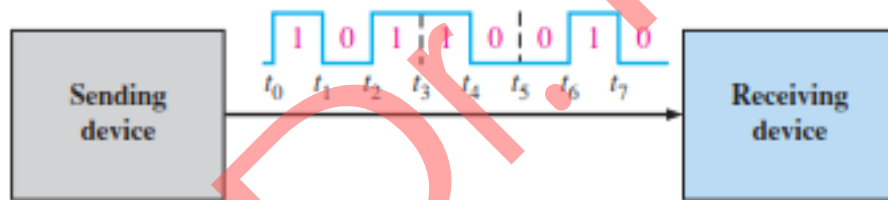
- A **timing diagram** is used to show the **relationship** between **two or more digital waveforms**, and **how** each waveform **changes** in relation to the others.



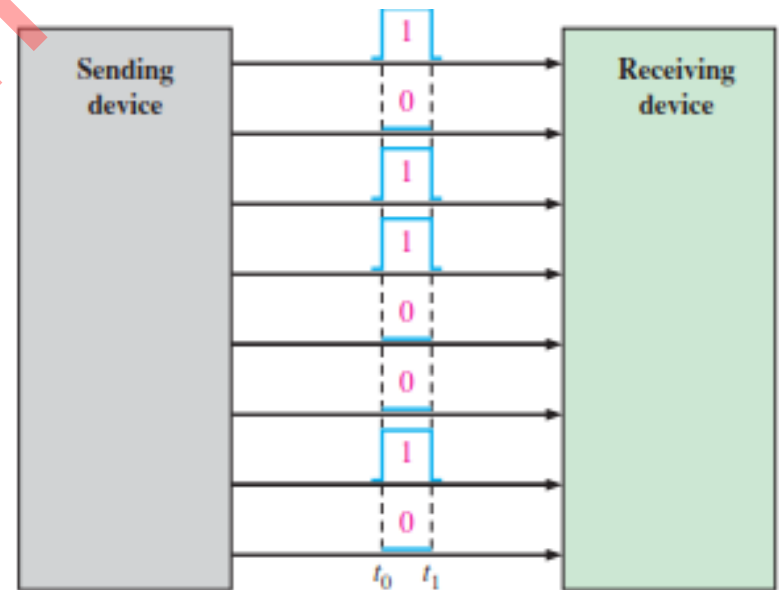
- From this **timing diagram** you can see, for example, that the three waveforms **A**, **B**, and **C** are **HIGH** only during **bit time 7** (shaded area) and they all change back **LOW** at the **end of bit time 7**.
- A diagram like this can be observed directly on a **logic analyzer**.

Data transfer

- **Data** refers to groups of bits that convey some type of information.
- **Binary data**, which are represented by digital waveforms, must be transferred from one to another within a digital system or from one system to another.
 - **For example**, numbers stored in binary form in the memory of a computer must be transferred to the computer's central processing unit in order to be added.
 - The sum of the addition must then be transferred to a monitor for display and/or transferred back to the memory.
 - Binary data are transferred in two ways: **serial** and **parallel**, as shown in Fig.



(a) Serial transfer of 8 bits of binary data. Interval t_0 to t_1 is first.



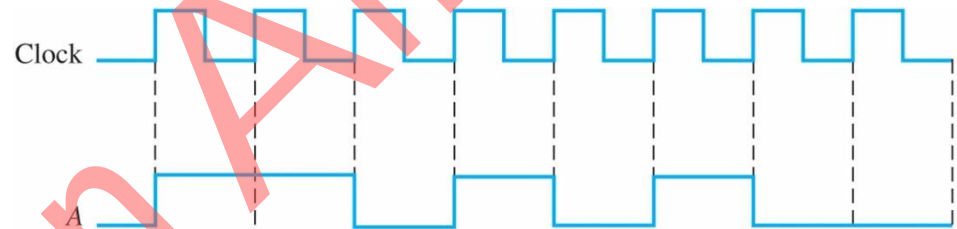
(b) Parallel transfer of 8 bits of binary data. The beginning time is t_0

Example 1-2

- a) Determine the total time required to **serially** transfer the *eight bits* contained in waveform **A** of Fig., and indicate the sequence of bits. The left-most bit is the first to be transferred. The 100 kHz clock is used as reference.
- b) What is the total time to transfer the same eight bits in **parallel**?

Solution

- a) The period is: $T = \frac{1}{f} = \frac{1}{100\text{kHz}} = 10\mu\text{s}$



It takes $10\mu\text{s}$ to transfer each bit in the waveform.

The total transfer time for eight bits is $8 \times 10\mu\text{s} = 80\mu\text{s}$

To determine the sequence of bits, examine the wave form during each bit time.

If waveform A is HIGH during the bit time, a 1 is transferred.

If waveform A is LOW during the bit time, a 0 is transferred.

The bit sequence is



The left-most bit is the first to be transferred

- b) A parallel transfer would take $10\mu\text{s}$ for all eight bits.



The end of Lecture_01, chapter 1

Problems & Solutions

Problem 1-1

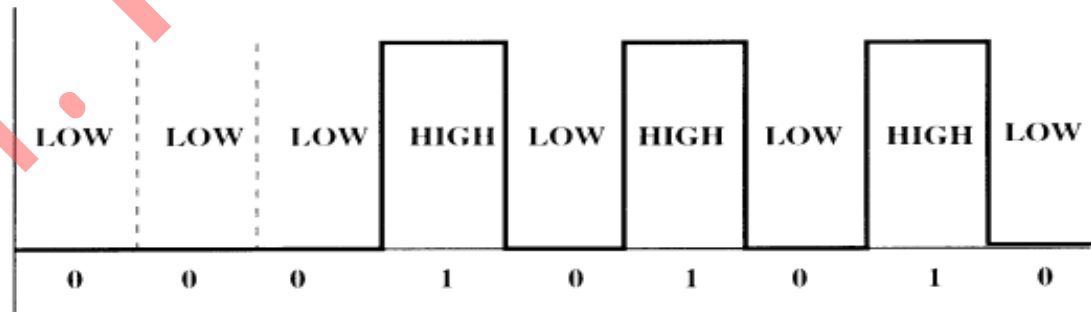
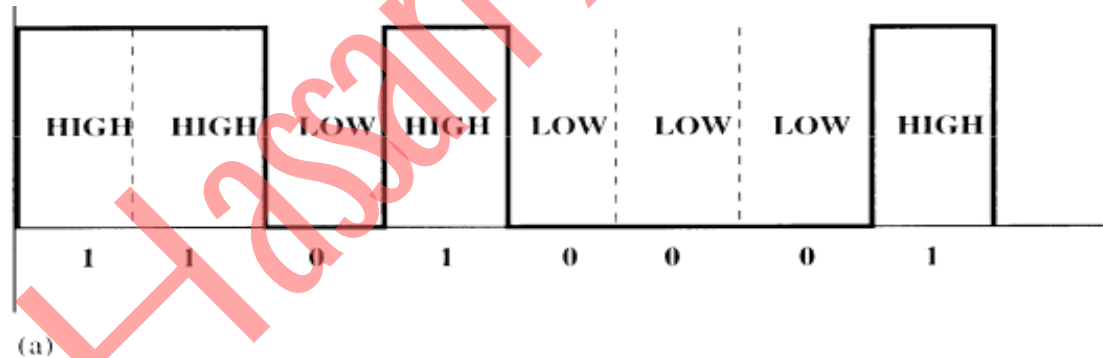
Define the sequence of bits (1s and 0s) represented by each of the following sequences of levels:

(a) HIGH, HIGH, LOW, HIGH, LOW, LOW, LOW, HIGH

(b) LOW, LOW, LOW, HIGH, LOW, HIGH, LOW, HIGH, LOW

Solution

HIGH = 1; LOW = 0. See Figure



Problem 1-2

Determine the duty cycle of the waveform in Fig.

Solution

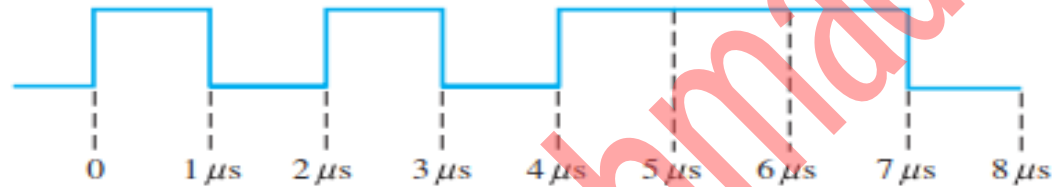


$$t_w = 2 \text{ ms}; T = 4 \text{ ms}$$

$$\text{Duty cycle} = \left(\frac{t_w}{T} \right) 100\% = \left(\frac{2\text{ms}}{4\text{ms}} \right) 100\% = 50\%$$

Problem 1-3

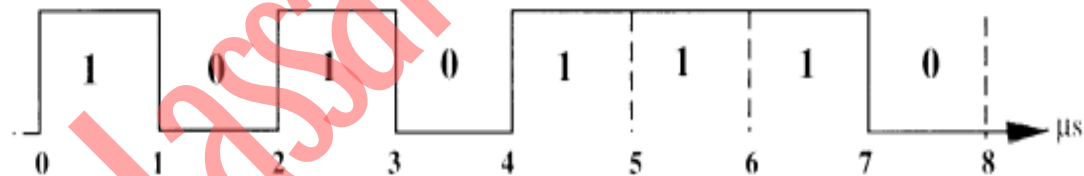
Given the waveform in Fig.



1. Determine the bit sequence represented by A bit time is 1 μs in this case
2. What is the total serial transfer time for the eight bits in Fig.? What is the total parallel transfer time?
3. What is the period if the clock frequency is 4 kHz?

Solution

- The bit sequence is:



- Each bit time = 1 μs , \Rightarrow Serial transfer time = (8 bits)(1 μs/bit) = 8 μs;
Parallel transfer time = 1 bit time = 1 μs
- The period:

$$T = \frac{1}{f} = \frac{1}{4\text{kHz}} = 0.25\text{ms}$$